

**PHYSICS - I
(PHYS 1001)**

Time Allotted : 3 hrs

Full Marks : 70

Figures out of the right margin indicate full marks.

Candidates are required to answer Group A and any 5 (five) from Group B to E, taking at least one from each group.

Candidates are required to give answer in their own words as far as practicable.

**Group - A
(Multiple Choice Type Questions)**

1. Choose the correct alternative for the following: **10 × 1 = 10**

- (i) A vector field $\vec{v}(x, y, z) = f(y)\hat{i} + g(x)\hat{j}$ is necessarily
 (a) irrotational (b) sink
 (c) source (d) solenoidal.
- (ii) Div curl \vec{A} is equal to
 (a) $\vec{\nabla} \times (\vec{\nabla} \times \vec{A})$ (b) $\vec{\nabla} \cdot \vec{A} + \vec{\nabla} \times \vec{A}$
 (c) $\vec{\nabla} \cdot \vec{A}$ (d) zero.
- (iii) Which of the following force law represents a central force?
 (a) $\vec{F} = k\cos^2\theta\hat{r}$ (b) $\vec{F} = -\frac{k}{r^2}\cos\theta\hat{r}$
 (c) $\vec{F} = -\frac{k}{r^3}\hat{r}$ (d) $\vec{F} = -\frac{k}{r^3}\hat{\theta}$.
- (iv) Mathematically, Coriolis acceleration is given by
 (a) $\ddot{\vec{r}}$ (b) $2\vec{\omega} \times \dot{\vec{r}}$ (c) $2\dot{\vec{r}} \times \vec{\omega}$ (d) $\vec{\omega} \times (\vec{\omega} \times \vec{r})$,
 where the terms have their usual meaning and overhead dot gives time derivative.
- (v) In a free-damped motion the relaxation time increases with the
 (a) increase in frequency (b) increase in damping factor
 (c) decrease in frequency (d) decrease in damping factor.
- (vi) In case of forced oscillation, the amplitude resonance frequency
 (a) increases with damping factor
 (b) decreases with damping factor
 (c) increases with time
 (d) decreases with time.

- (vii) Number of optic axis in a uniaxial crystal is
 (a) one (b) two (c) five (d) three.
- (viii) A polarized wave given by light vector $\vec{E}(z, t) = E_0 \cos(\omega t - kz)\hat{i} + E_0 \sin(\omega t - kz)\hat{j}$ is
 (a) linearly polarized wave (b) elliptically polarized wave
 (c) circularly polarized wave (d) plane polarized wave.
- (ix) The dimension of polarizability in SI unit is
 (a) Fm^2 (b) Fm (c) Fm^{-1} (d) Fm^{-2} .
- (x) At a very large distance the electric field on the axis of a uniformly charged circular ring behaves like that of a
 (a) dipole (b) quadrupole
 (c) neutral object (d) point charge.

Group - B

2. (a) A surface is given by the equation $z^2 = x^2 + y^2$. Find a unit normal at the point (1, 0, -1).
 (b) If \vec{r} is the vector from some fixed point (x_0, y_0, z_0) to the point (x, y, z) and r is its length, show that $\vec{\nabla}(r^2) = 2\vec{r}$.
 (c) (i) Show that a vector field given by an equation $\vec{E}(x, y, z) = (2xy + z^3)\hat{i} + x^2\hat{j} + 3xz^2\hat{k}$ is irrotational.
 (ii) Calculate the divergence of the same vector field at a point (1, 0, 1).
 (iii) Show that for a scalar field Ψ , $\vec{\nabla} \times \vec{\nabla}\Psi = \vec{0}$.
- 3 + 2 + (2 + 2 + 3) = 12**
3. (a) Show that for a particle undertaking motion in a central force field, angular momentum remains conserved.
 (b) The orbit of a particle under the influence of a central force is given by $r = e^{-\theta}$. Find out the corresponding force law.
 (c) Write Kepler's laws of planetary motion.
 (d) What is Coriolis force? Under what conditions do we get non-zero Coriolis acceleration?
- 3 + 3 + 3 + (2 + 1) = 12**

Group – C

4. (a) A damped harmonic oscillation performed by a particle is given by the following equation:

$$\frac{d^2x}{dt^2} + 2\pi \frac{dx}{dt} + \omega_0^2 x = 0.$$

- (i) Write down the condition for which the motion will represent a weakly damped oscillation.
 (ii) Find out the value of its logarithmic decrement.
- (b) Write down the differential equation of forced vibration mentioning each and every term.
- (c) Obtain mathematically the expression for the amplitude resonance frequency. Show graphically how amplitude resonant frequency shifts on the frequency axis with the decrease of damping.

$$(2 + 3) + (1 + 1) + (3 + 2) = 12$$

5. (a) Find the state of polarization when the x and y components of the electric field are given by $E_x = E_0 \sin(\omega t + kz)$ and $E_y = E_0 \cos(\omega t + kz)$.

- (b) Does $y = A \sin^2(kx - \omega t)$ represent a progressive harmonic wave? Justify your answer.
- (c) Explain briefly the phenomenon of population inversion.
- (d) State the physical significance of Einstein's A and B coefficient in LASER and find relation between them.

$$3 + (2 + 1) + 3 + 3 = 12$$

Group – D

6. (a) Two point charges q and $2q$ are located at $(1, 1)$ and $(1, -1)$. Find the field and potential at the origin $(0, 0)$.
- (b) Calculate electric potential due to a uniformly charged ring of diameter 2cm and total charge 1C at a point on the axis of the ring at a distance of 1m if the ring is placed in xy -plane at $z = 0$.
- (c) Obtain Poisson equation starting from differential form of Gauss's law of electrostatics.
- (d) The potential due to a spherically symmetric charge distribution is given by $\Psi(r) = \frac{ke^{-r}}{r}$, k being a constant. Find out the charge density of this distribution.

$$(2 + 2) + 3 + 2 + 3 = 12$$

7. (a) (i) State the Laplace's equation in electrostatics.
 (ii) Under what condition does Poisson's equation reduce to Laplace's equation?
- (b) Following Laplace's equation obtain the expression for electrostatic field within the region of two conducting spheres of radii a and b where the outer one is earthed. Also, assume that potential of the inner sphere is V_1 volt.
- (c) Derive the expression of atomic polarizability for a neutral atom.
- (d) The dielectric constant of Helium at 0°C is 1.0000684. If the gas contains 2.7×10^{24} atoms/ m^3 , find the radius of the electron cloud.

$$(1 + 2) + 4 + 3 + 2 = 12$$

Group – E

8. (a) Write down Biot-Savart law of magnetostatics. Using the law obtain the expression for magnetic field produced due to an infinitely long conductor carrying current along \hat{k} .
- (b) In case of a linear medium show that $\mu = \mu_0(1 + \chi_m)$, where the symbols have their usual meaning.
- (c) A magnetic field $4 \times 10^{-3} \hat{k}$ tesla exerts a force of $(4\hat{i} + 3\hat{j}) \times 10^{-10} \text{N}$ on a particle having charge of $1 \times 10^{-9} \text{C}$ and moving in x - y plane. Calculate the velocity of the particle.
- (d) Obtain differential form of Faraday's law from its integral form.

$$(1 + 3) + 4 + 2 + 2 = 12$$

9. (a) (i) The vector potential corresponding to a magnetic field is given by $\vec{A}(\vec{r}) = C(y\hat{i} - x\hat{j})$, C is a constant scalar. Show that the said magnetic field is constant.
 (ii) Plot susceptibility vs temperature for a paramagnetic material and paramagnetic phase of a ferromagnetic material.
- (b) A square loop of side 'a' is placed parallel to xy -plane in presence of a vertical magnetic field along z -axis. The loop is carrying a current 'i'. Calculate the force acting on each side of the loop, magnetic moment of the loop and torque acting on the loop.

$$(3 + 3) + (2 + 2 + 2) = 12$$